

# Adaptive Oblivious Transfer with Access Control from Lattice Assumptions

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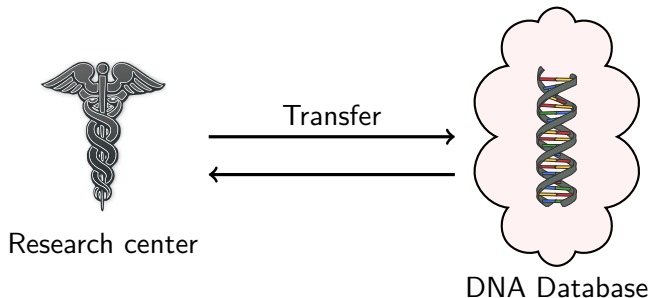
# Anonymous Databases



Research center

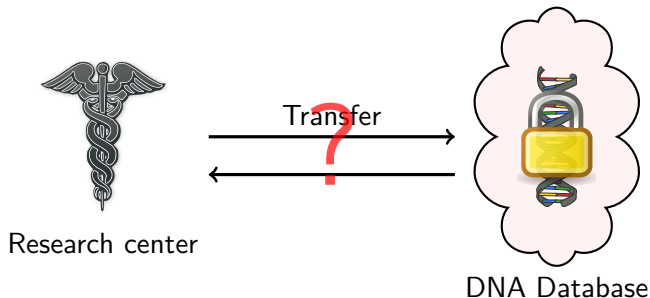
- ▶ DNA storage is expensive

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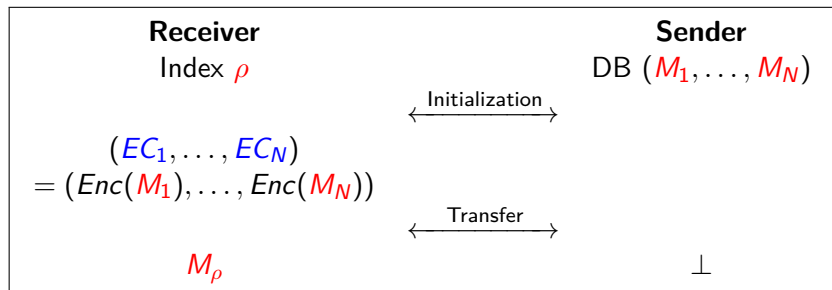
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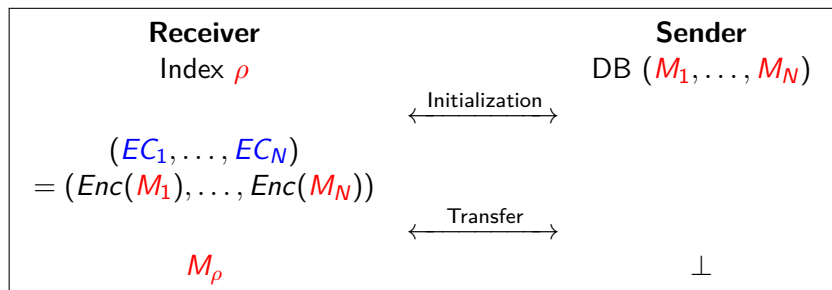


- ▶ DNA storage is expensive
  - ▶ DNA Database's requests are sensitive
- query-anonymous transfers

# (Adaptive) Oblivious Transfer (OT) [Chau81]

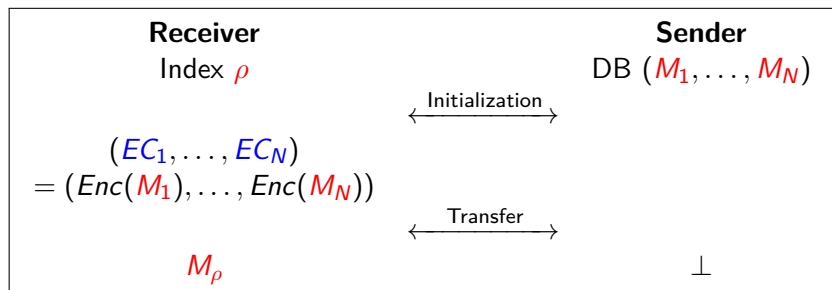


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- ▶ Complete building block of cryptography [GMW87]
- ▶ **Adaptive** OT: receiver adaptively obtains  $k$  messages [NP93]
  - Usage: Sensitive DB (DNA, financial data, ...).

# History

1981 [Chaum](#): introduction

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2008 [Green and Hohenberger](#): adaptive OT in the UC model

2009 [Camenisch, Dubovitskaya and Neven](#): access control

2011 [Green and Hohenberger](#): adaptive OT from pairings

► From FHE + OPRF, or PIR, or ad-hoc pairing assumptions. . .

**No fully simulatable adaptive OT with access control from lattice assumptions**

# Lattice-Based Cryptography [Ajt96, Reg05]

## Lattice

A lattice is a discrete subgroup of  $\mathbb{R}^n$ . Can be seen as integer linear combinations of a finite set of vectors.

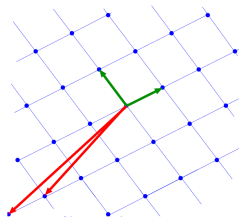
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## Why?

- ▶ Simple and asymptotically efficient;
- ▶ **Still** conjectured quantum-resistant;
- ▶ Connection between average-case and worst-case problems;
- ▶ Powerful functionalities (e.g., FHE).

→ Finding a short non-zero vector in a lattice is hard.

# Hardness Assumptions: SIS and LWE [Ajt96, Reg05]

**Parameters:**  $n$  dimension,  $m \geq n$ ,  $q$  modulus.

For  $\mathbf{A} \leftarrow \mathcal{U}(\mathbb{Z}_q^{m \times n})$ :

## Small Integer Solution

$$\mathbf{x} \mathbf{A} = \mathbf{0} [q]$$

**Goal:** Given  $\mathbf{A} \in \mathbb{Z}_q^{m \times n}$ , find  $\mathbf{x} \in \mathbb{Z}^m \setminus \{\mathbf{0}\}$  small

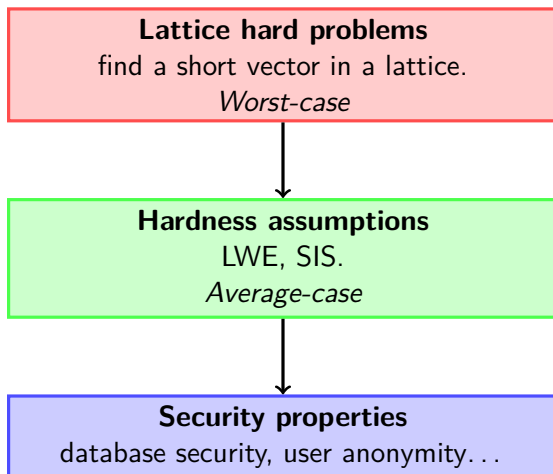
## Learning With Errors

$$\left( \begin{array}{c} m \\ \mathbf{A} \end{array}, \mathbf{A} \mathbf{s} + \mathbf{e} \right)$$

$\mathbf{s} \leftarrow \mathbb{Z}_q^n$      $\mathbf{e}$  small error

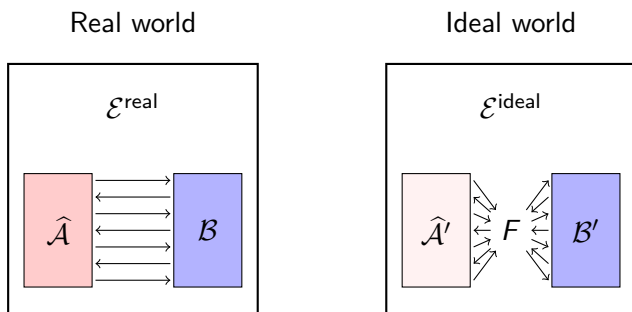
**Goal:** Given  $(\mathbf{A}, \mathbf{A} \mathbf{s} + \mathbf{e})$ , find  $\mathbf{s} \in \mathbb{Z}_q^n$

# Provable Security



# Full Simulation Model [\[Can01\]](#)

For any cheating  $\hat{\mathcal{A}}$ , there exists  $\hat{\mathcal{A}}'$  s.t.



$$\text{View}(\mathcal{E}^{\text{real}}) \approx_s \text{View}(\mathcal{E}^{\text{ideal}})$$

- Strictly stronger security model than indistinguishability-based one



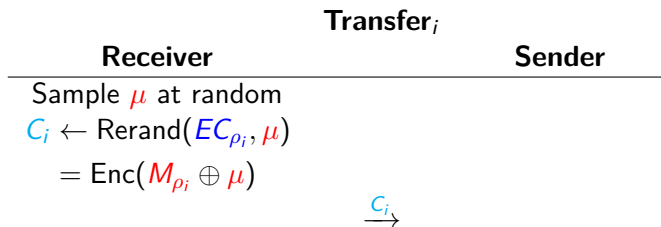
# Outline

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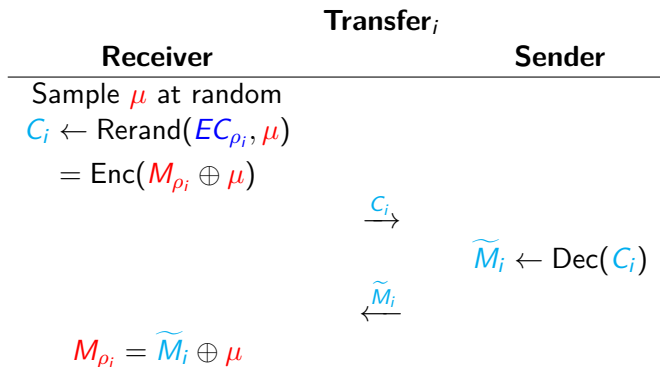
Building Blocks

Adaptive Oblivious Transfer with Access Control

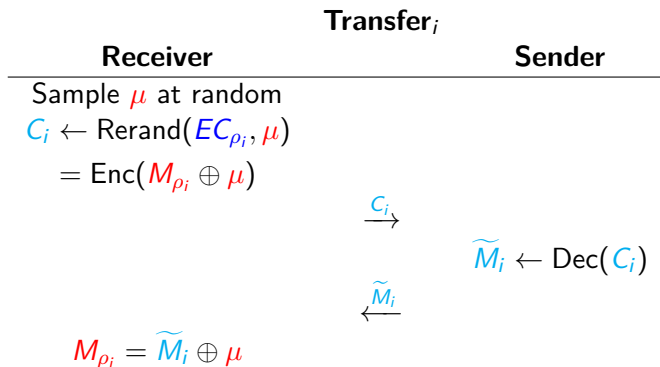
# Assisted Decryption Technique [CNs07]



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+ **Zero-knowledge proofs** compatible with the PKE (Keygen, Enc, Dec, Rerand)

# Regev's Encryption [Reg05]

## Keygen:

Secret key:  $\mathbf{S} \leftarrow \chi^{n \times t}$

Public key:  $(\mathbf{F}, \mathbf{P})$  s.t.  $\mathbf{F} \leftarrow U(\mathbb{Z}_q^{n \times m})$ ,  $\mathbf{P} = \mathbf{F}^T \mathbf{S} + \mathbf{E}$

with  $\mathbf{E} \leftarrow \chi^{m \times t}$

**Encryption:**  $(\mathbf{a}, \mathbf{b}) = (\mathbf{a}, \mathbf{S}^T \mathbf{a} + \mathbf{x} + M \lfloor \frac{q}{2} \rfloor) \in \mathbb{Z}_q^n \times \mathbb{Z}_q^t$

**Decryption:**  $M = \lfloor (\mathbf{b} - \mathbf{S}^T \cdot \mathbf{a}) / (\frac{q}{2}) \rfloor$

**Rerand:**  $(\mathbf{a}', \mathbf{b}') = (\mathbf{a} + \mathbf{F} \mathbf{e}, \mathbf{b} + \mathbf{P}^T \mathbf{e} + \mu \lfloor \frac{q}{2} \rfloor) = \text{Enc}(M \oplus \mu)$

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+ ZK proofs

# Smudging [\[AJL+12\]](#)

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### Attack scenario:

- ▶  $DB = (M_0, M_1)$
- ▶ Sender encrypts  $M_0$  with noise  $\mathbf{x}_0$  and  $M_1$  with noise  $\mathbf{x}_1$  s.t.  
 $\|\mathbf{x}_0\| \ll \|\mathbf{x}_1\| \leq B_\chi$
- ▶ Upon receiving  $(\mathbf{c}_0, \mathbf{c}_1)$ , decryption leaks  $\|\mathbf{x}_i + \mathbf{e}\|$

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**Solution:** Flood the noise with  $\nu$  s.t.  $\|\nu\| \gg B_\chi$ .

**Rerand:**  $(\mathbf{a}', \mathbf{b}') = (\mathbf{a} + \mathbf{F} \mathbf{e}, \mathbf{b} + \mathbf{P}^T \mathbf{e} + \mu \lfloor \frac{q}{2} \rfloor + \nu)$

## AC-OT

Encrypted database consists in  $(EC_i, AP_i)_{i=1}^N$ .

Receiver can retrieve message  $M_i$  iff it possesses  $\text{cert}_x$  for some  $x \in \{0, 1\}^*$  s.t.  $AP_i(x) = 1$ .

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[ACDN13]: access policy made of conjunctions:  $x_1 \wedge \dots \wedge x_\ell$ .

Disjunctions possible through replication.

[ZAW+10]: use CP-ABE to handle  $\text{NC}^1$  access policies.

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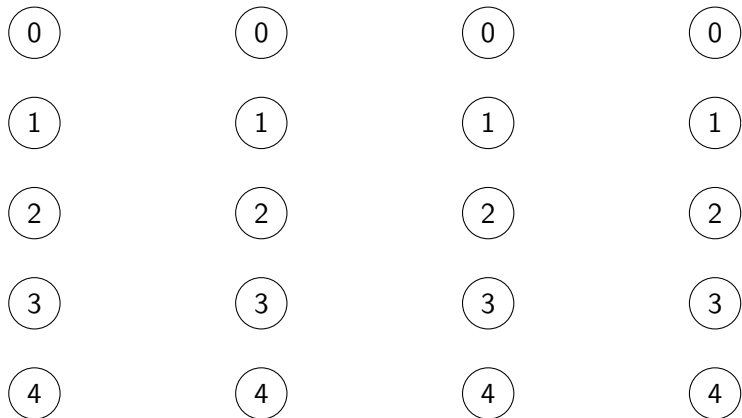
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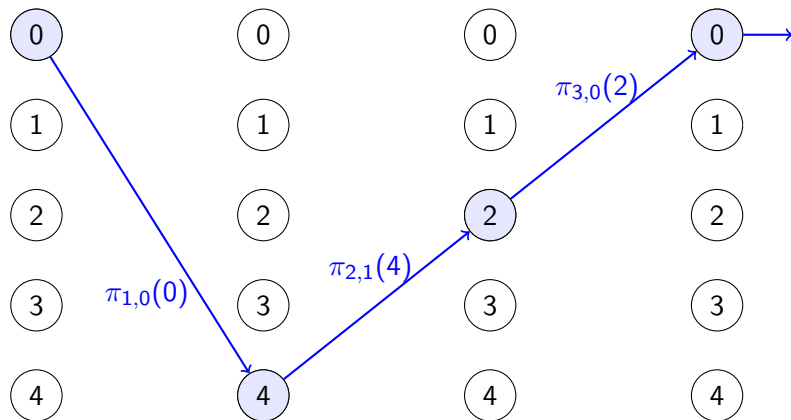
[ZAW+10]: use CP-ABE to handle  $\text{NC}^1$  access policies.

**Here:** access policy made of **branching program** (BP).

# Branching Programs

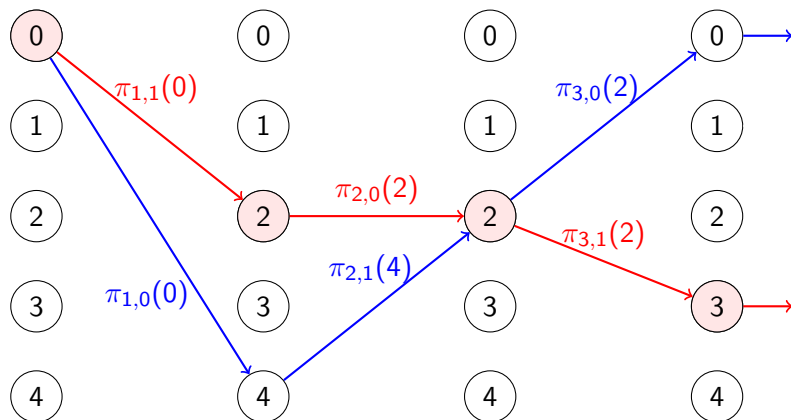


# Branching Programs



$x = 010$ : accepted

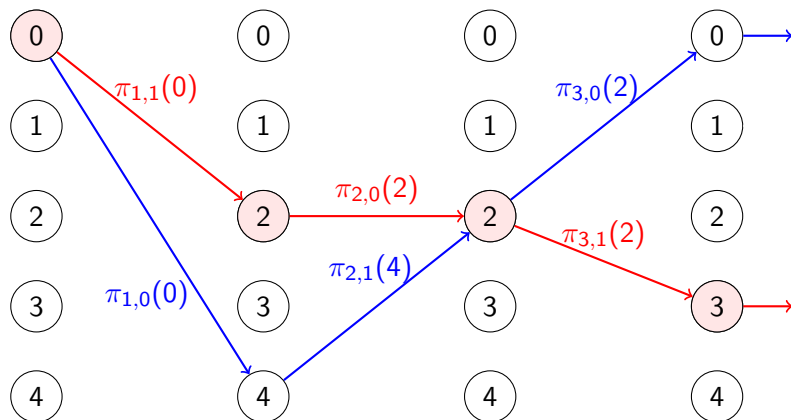
# Branching Programs



$x = 010$ : accepted

$y = 101$ : rejected

# Branching Programs




$x = 010$ : accepted  
 $y = 101$ : rejected

[Barr86]: polynomially-long BP  
are equivalent to  $NC^1$



# Branching Programs

$$\{(EC_1, BP_1), (EC_2, BP_2), \dots, (EC_N, BP_N)\}.$$




$(x, cert_x)$

**Goal:** Prove knowledge of  $cert_x = \text{Sign}(x)$  s.t.  $\exists i : BP_i(x) = 1$ .

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**This work:** Make BP's statements work with Stern's proofs [Ste93]

# Branching Programs

## Encoding of a branching program:

$$\mathbf{z}_{BP} = (d_{1,1}, \dots, d_{1,\delta_\kappa}, \dots, d_{L,1}, \dots, d_{L,\delta_\kappa}, \pi_{1,0}(0), \dots, \pi_{1,0}(4), \pi_{1,1}(0), \dots, \pi_{1,1}(4), \dots, \pi_{L,0}(0), \dots, \pi_{L,0}(4), \pi_{L,1}(0), \dots, \pi_{L,1}(4)) \in [0, 4]^\zeta$$

$d_{\theta,1}, \dots, d_{\theta,\delta_\kappa}$ : bit representation of  $\text{var}(\theta)$

## Step-by-step evaluation:

$$\eta_\theta = \pi_{\theta, x_{\text{var}(\theta)}}(\eta_{\theta-1}) = \pi_{\theta,0}(\eta_{\theta-1}) \cdot \bar{x}_{\text{var}(\theta)} + \pi_{\theta,1}(\eta_{\theta-1}) \cdot x_{\text{var}(\theta)}$$

Proving correct evaluation

**Naively:** prove each step  $\rightarrow O(L \cdot \kappa)$

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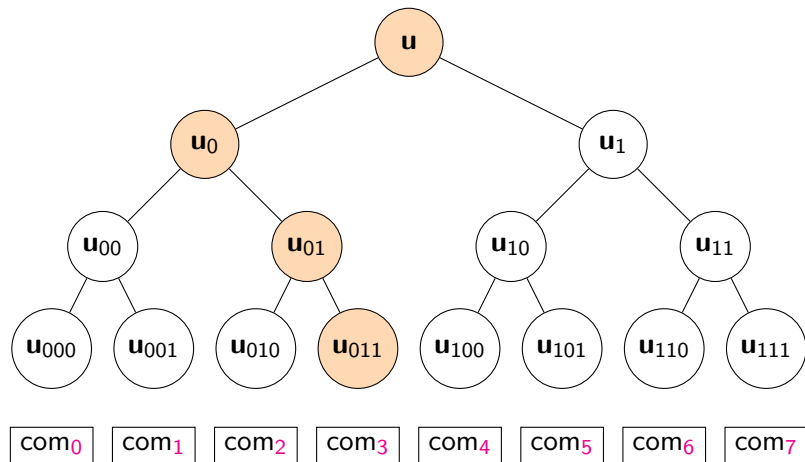
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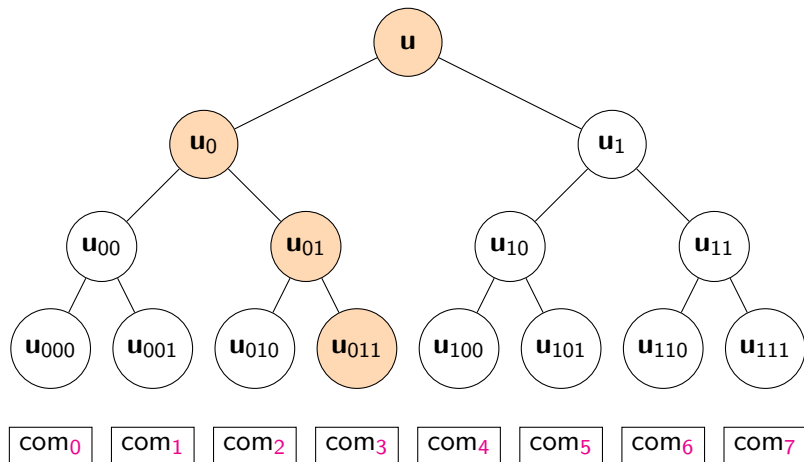
**Our idea:** use binary-search  $\rightarrow O(L \cdot \log(\kappa))$

# Branching Programs



$$com_i = Com(x_i)$$

# Branching Programs



$com_i = Com(x_i) \rightarrow$  correct binary search  $\Rightarrow$  knowledge of  $x_{var(\theta)}$

# Commitments

Digital equivalent of a sealed box.



e.g., Pedersen Commitment

$$pk = (g, h) \leftarrow \mathbb{G}^2$$

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## Properties

Commitments provide

- ▶ **Binding** property: once sealed, a value cannot be changed
- ▶ **Hiding** property: nobody is able tell what is inside the box without the key



# Zero-Knowledge (ZK) Proofs

## Definition

A ZK proof is an interactive protocol between prover  $P$  and verifier  $V$  that verifies:

**Completeness:** Correctness of the protocol.

**Soundness:** No cheating prover can convince the verifier.

**Zero-Knowledge:** Verifier learns nothing but the validity of the statement.

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- ▶ Non interactive variant exists: NIZK proofs
- ▶ Random-Oracle Model: transform from ZK to NIZK [FS86]
- ▶ Standard Model: Groth-Sahai for pairing-based crypto [GS08]

# Zero-Knowledge Proofs for Lattices

No equivalent of Groth-Sahai proofs!

Reason

Lattices propose less algebraic structure than pairing groups.

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Lattices propose less algebraic structure than pairing groups.

Two main proof systems in lattice-based cryptography:

Lyubashevky like [Lyu09]: On Ring-LWE, concise but not expressive.  
Algebraic

Stern like [Ste93]: On LWE, heavy but expressive.  
Combinatorial

Both are interactive.

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[KTX08]: mod 2  $\rightarrow$  mod  $q$

[LNSW13]: Extends Stern's protocol for SIS and LWE statements

Recent uses of Stern-like protocols in lattice-based crypto:

[LNW15, LLNW16, LLNMW16a, LLNMW16b, LLNW17]

## Signature with Efficient Protocols [CL02]

A signature scheme (**Keygen**, **Sign**<sub>sk</sub>, **Verif**<sub>vk</sub>) with companion protocols:

- ▶ **Sign** a committed value;
- ▶ Prove possession of a signature in **ZK**.



# Signature with Efficient Protocols [CL02]

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## Security

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We use a SIS-based construction from Asiacrypt'16 [\[LLNMW16\]](#).

# Outline

Introduction

Building Blocks

Adaptive Oblivious Transfer with Access Control

# Our Construction

## Ingredients

- ▶ The assisted decryption technique
- ▶ A simplification of [LLNMW16]'s signatures as certificates
- ▶ Access control using BP
- ▶ WI proofs *à la* Stern

# Our Adaptive Oblivious Transfer Construction

## Initialization

Sender side:

1. Generate  $(VK_{sig}, SK_{sig}) \leftarrow \Sigma.keygen(1^\lambda)$
2. Compute  $((\mathbf{S}, \mathbf{E}), (\mathbf{F}, \mathbf{P})) \leftarrow Regev.keygen(1^\lambda)$
3. Use  $\mathbf{S}$  to compute encryptions of  $M_i \rightarrow (\mathbf{a}_i, \mathbf{b}_i) \in \mathbb{Z}_q^n \times \mathbb{Z}_q^t$
4. Use  $SK_{sig}$  to compute signatures of  $(\mathbf{a}_i, \mathbf{b}_i) \rightarrow \sigma_i$
5.  $EC_i \leftarrow (\sigma_i, (\mathbf{a}_i, \mathbf{b}_i))$

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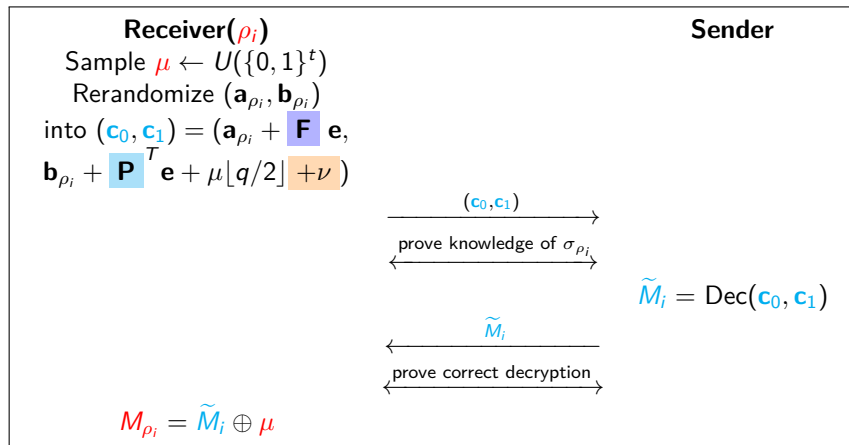
Sender sends  $(VK_{sig}, (\mathbf{F}, \mathbf{P}), EC_i)$  to the Receiver and proves that everything was done correctly.

Sender keeps the previous information and  $(\mathbf{S}, \mathbf{E})$ .



# Our Adaptive Oblivious Transfer Construction

## Transfer



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## Final steps

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## Final steps

- ▶ Access control can be plug in our scheme
- ▶ Our scheme is proven secure in the standard model
  - In the ROM: optimizations using NIWI proofs [\[FS86\]](#)

# Comparison

## Adaptive OT with Access Control

Protocol	Initialization Cost	Transfer Cost	Assumptions	Policies	Private Policies	Security
CDN09	$\mathcal{O}(\lambda \cdot N)$	$\mathcal{O}(\lambda) \cdot \text{Poly}(\lambda)$	$q$ -type	Conj.	✗	Full-Sim
CDNZ11	$\mathcal{O}(\lambda \cdot N)$	$\mathcal{O}(\lambda) \cdot \text{Poly}(\lambda)$	$q$ -type + XDDH	Conj.	✓	Full-Sim
ACDN13	$\mathcal{O}(\lambda \cdot N)$	$\mathcal{O}(\lambda) \cdot \text{Poly}(\lambda)$	DLIN + SXDH	Conj.	✗	UC
ZAW+10	$\mathcal{O}(\lambda \cdot N)$	$\mathcal{O}(\lambda)$	CP-ABE + $q$ -type	NC <sup>1</sup>	✗	Full-Sim
CDEN12	$\mathcal{O}(\lambda \cdot N)$	$\mathcal{O}(\lambda \log N) + \text{Poly}(\lambda)$	CP-ABE + GGM	CNF <sup>-</sup>	✓	Full-Sim
Ours	$\mathcal{O}(\lambda \cdot N)$	$\widetilde{\mathcal{O}}(\lambda \log N) + \text{Poly}(\lambda)$	LWE + SIS	NC <sup>1</sup>	✗	Full-Sim

CNF<sup>-</sup> is a restricted version of CNF:  $\text{AP}(EC) = \bigwedge_i \bigvee_j x_{i,j}$  where each  $x_{i,j}$  belongs to a given category  $C_i$  (e.g. {Surgeon, Nurse, Administrative}).

# Conclusion

- ▶ First AC-OT in the lattice setting that handles expressive statements ( $\text{NC}^1$ )
- ▶ Rely on LWE with superpolynomial modulus
- ▶ Proved in the full simulation model

## **Possible improvements:**

- ▶ Remove smudging
- ▶ Improve efficiency

